

Grid computing simulation of superconducting vortex lattice in superconducting magnetic nanostructures

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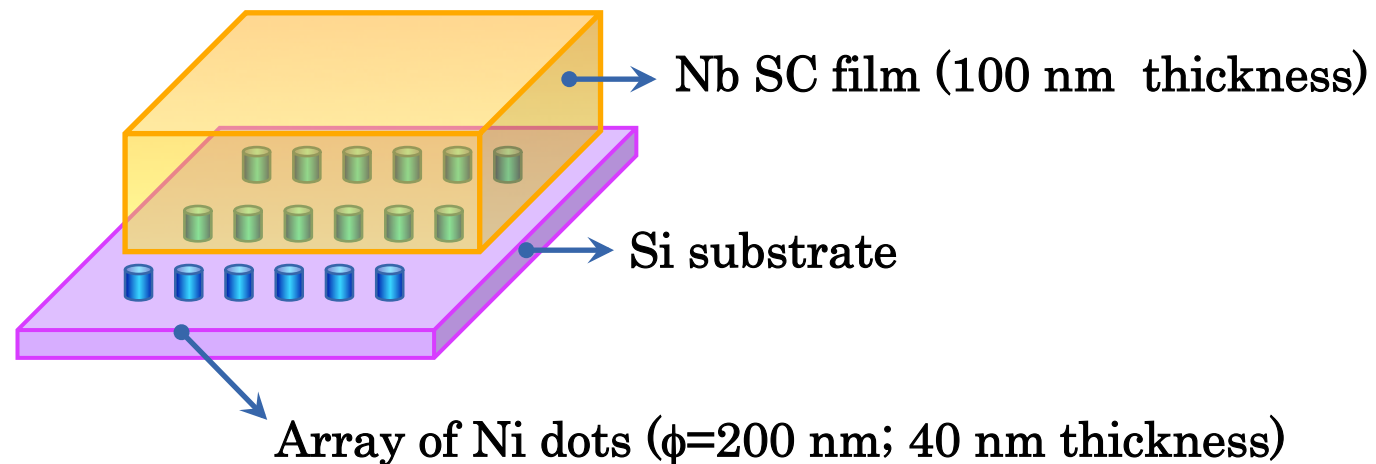
Braga, May 24th-27nd 2010



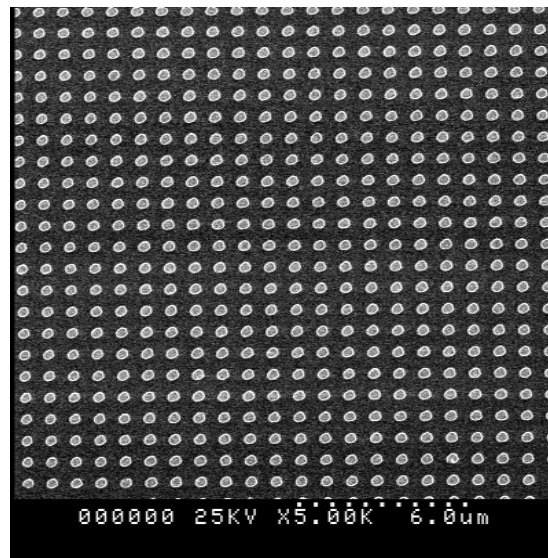
- **Introduction**
- **The DiVoS code and its Physics**
- **Implementation**
 - Complete DiVoS
 - Optimised DiVoS
 - Division of the problem
 - Architecture of the proposed solution
- **Results**
 - Testbed
 - Performance
- **Conclusions**



- **Superconducting (SC) Vortices Lattices (VL) are modified if nanodefects are embedded in SC samples**
 - Engineering applications
 - SC amorphous Mo_3Si (a- Mo_3Si) and Nb films on arrays of Ni nanodots

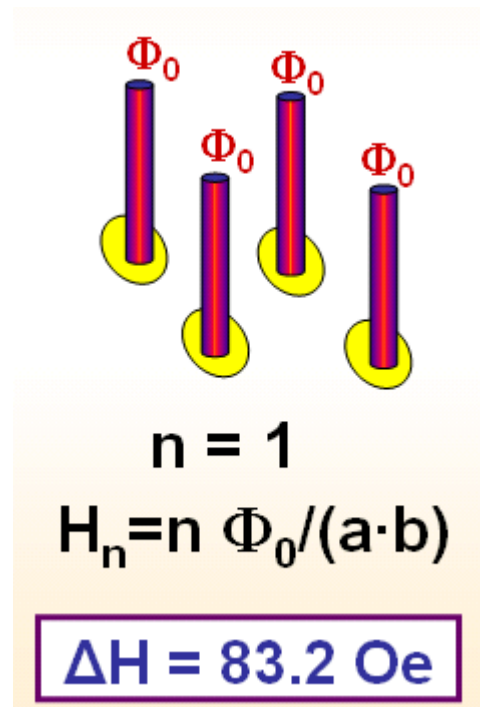


- **Several effects reported**
 - Induction by arrays made with different materials
 - Different diameters of the pinning centres
 - Arrays with different symmetries
 - Softening the strength of the intrinsic random pinning potentials



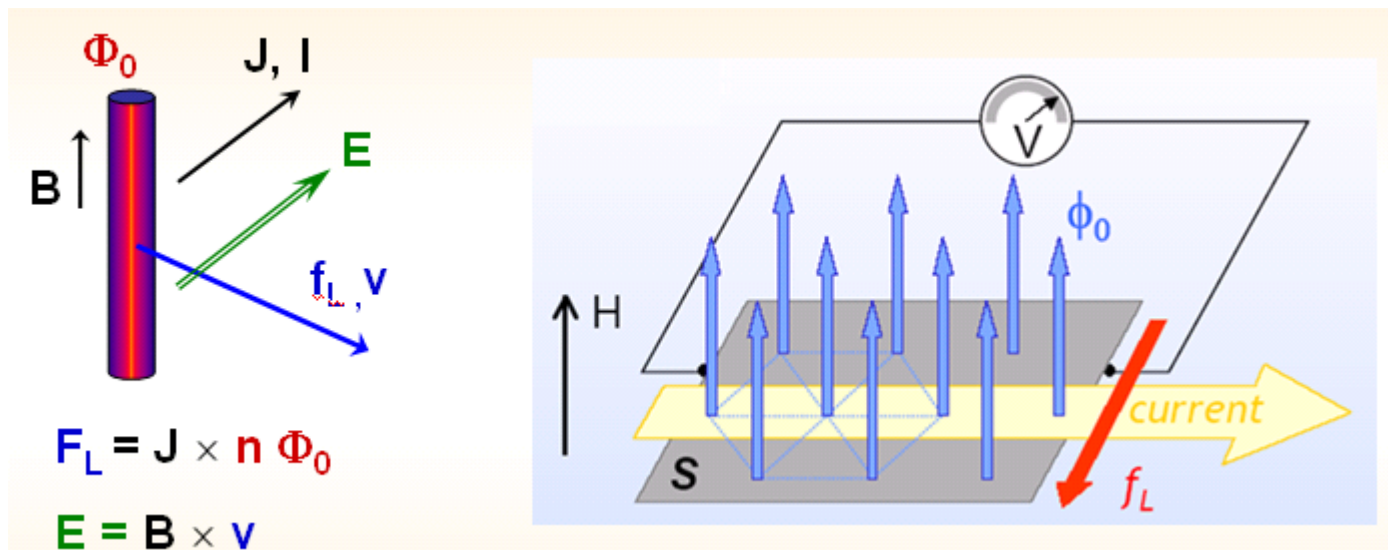
Lithography by electron beam

- **Experimental VL**
 - 400 x 600 nm² and 400 x 400 nm²
 - The simplest case has Matching Field (MF) equal to 1

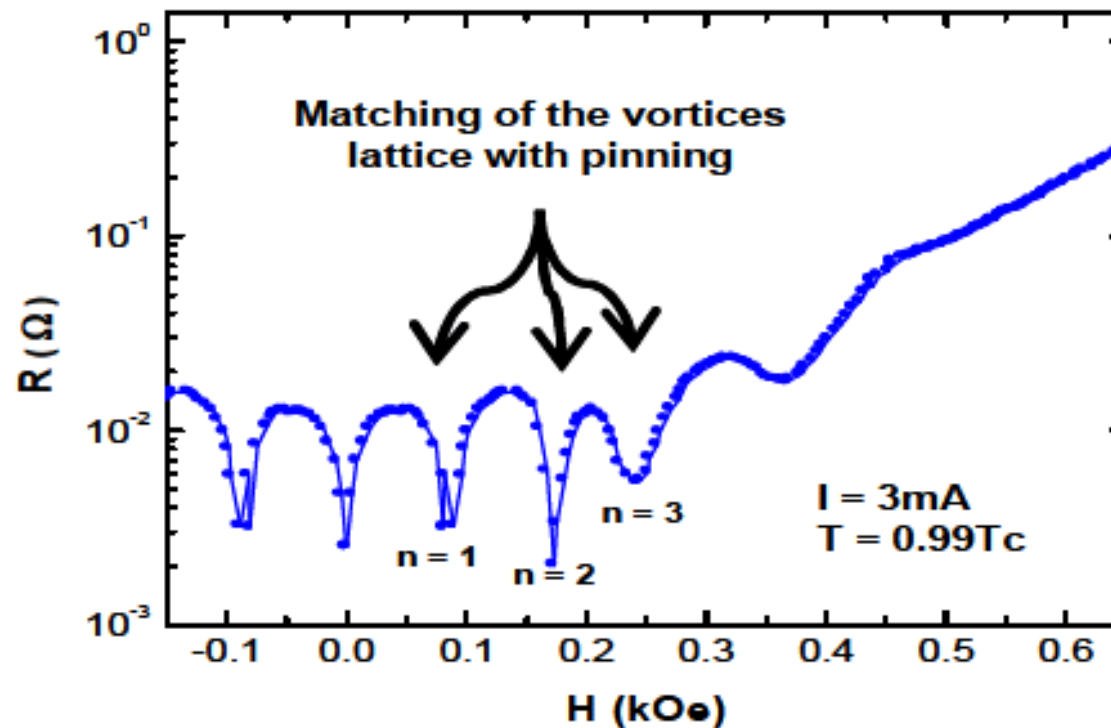


Array minima at these
magnetic fields

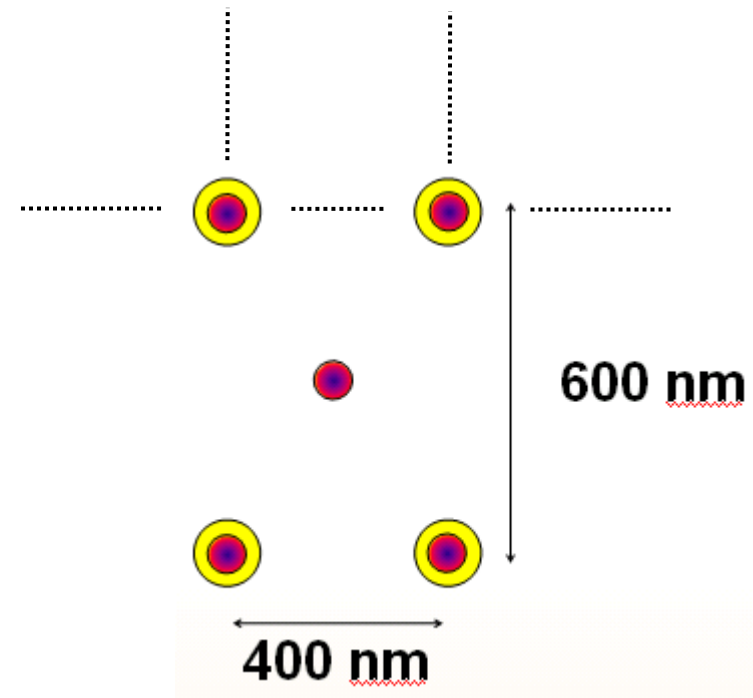
- Appliance of magnetic fields perpendicularly
- VL accommodates to the nanostructured arrays
- Vortices are moved because of Lorentz Force
- An Electric Field is then originated due to the velocity of the lattice



- Magnetoresistance of superconducting thin films with periodic arrays of pinning centres show minima when the vortex lattice matches the unit cell of the array

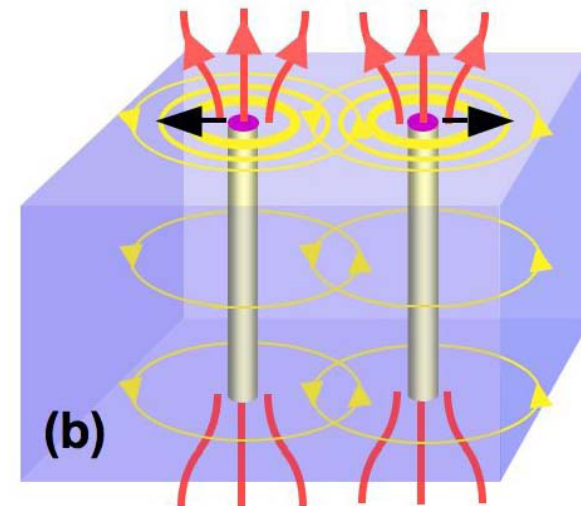


- **Dinámica de Vórtices Superconductores (DiVoS) code**
 - Fortran95
 - Study the VL dynamics in a Type-II SC
 - Simulates the observed phenomena by increasing the MF
 - The number of vortices depending on their position
 - *Vertex counts for 1/4*
 - *Edge counts for 1/2*
 - *Inner counts for 1*



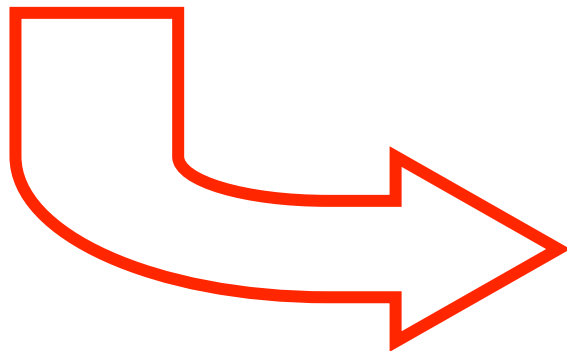
- Dinámica de Vórtices Superconductores (DiVoS) code
 - Vortex-Vortex interaction

$$U_{ij}(\mathbf{r}_{ij}) = \frac{\phi_0^2}{8\pi^2\lambda^3} K_0 \left(\frac{r_{ij}}{\lambda} \right)$$



- **Dinámica de Vórtices Superconductores (DiVoS) code**
 - Retrieves the lowest Energy configuration
 - Any MF configuration will have MF solutions
 - Running from $MF - 1$ to $2 \cdot (MF - 1)$
 - The space of solutions is

$$C_{(a \times b), V_p} = \frac{(a \times b)!}{V_p!((a \times b) - V_p)!}$$



Matching Field	Number of solutions
2	$2.380 \cdot 10^5$
3	$2.832 \cdot 10^{10}$
4	$2.247 \cdot 10^{15}$
5	$1.337 \cdot 10^{20}$
6	$6.364 \cdot 10^{24}$
7	$2.524 \cdot 10^{29}$

400 x 600 lattice

- **Dinámica de Vórtices Superconductores (DiVoS) code**
 - Two versions
 - Complete → All possible combinations are calculated
 - Optimized → Heuristics are used
 - Symmetry → Σr_{ij} is constant
 - Minimum Distance between vortices equal to a/V_p

- **Division of the problem**

- The evaluation of each solution is independent from the rest
- Any vortex can be placed on a (X, Y) position in an axb lattice
- S_p independent partitions with s_p subtasks
- The different positions satisfy:

$$((X \cdot a + Y) \bmod S_p) = s_p$$

running the a dimension

- **Architecture**

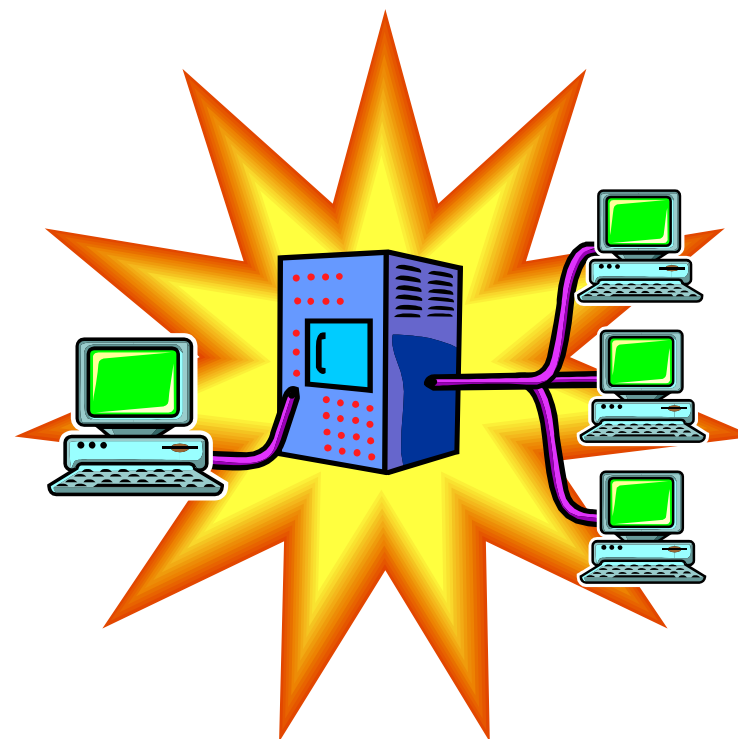
- Static compilation of 32 bits-X86 enabled version
- Bessel function by NAG Library¹
- Submission of jobs by GridWay²
 - Python script for analysing partial results



¹ <http://www.nag.co.uk/numeric/FL/FLdocumentation.asp>

² E. Huedo *et al.* *Software-Practice & Experience* **34**, 631 (2004)

- **Testbed**
 - Local cluster
 - Euler
 - Grid
 - EGEE Infrastructure



- **Euler characteristics**

- 144 blades with 2 Xeon 5450 quad-core 3.0 GHz
- 2 GB RAM/core
- Double Infiniband 4X DDR
- $R_{\text{peak}} = 13.82$ Tflops ; $R_{\text{max}} = 10.98$ Tflops
- Queue policy
 - 104 free slots
 - Serial jobs < 70%

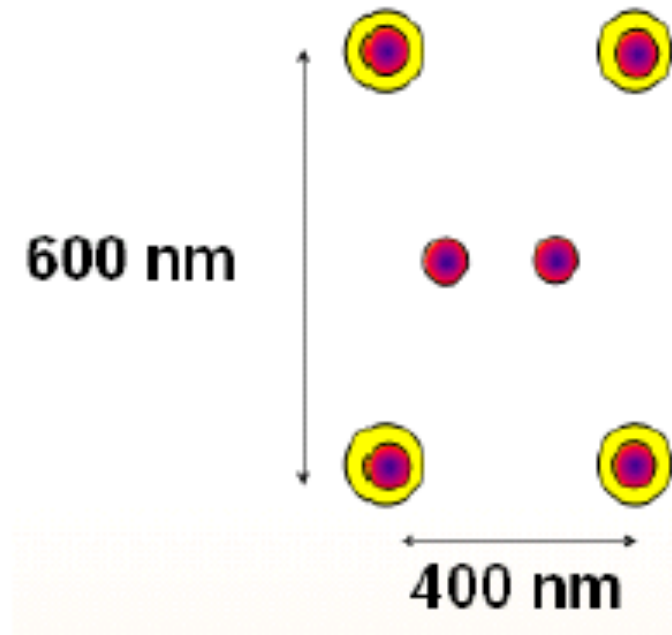
Name of the queue	Walltime [h]
pruebas	00 : 10 : 00
expres	02 : 30 : 00
normal	100 : 00 : 00
eterna	240 : 00 : 00



- **EGEE Infrastructure**
 - 29 sites
 - 16371 CPU
 - Free < 6010
 - Limitation of number of jobs per user
 - $90 < \text{Number of slots} < 110$



- A physical result as an example...
 - MF = 3
 - Two inner vortices
 - Four vertex vortices
 - 400 x 600 nm²
 - $U_{ij}(r_{ij}) = 5.83 \cdot 10^{-28} \text{ T}^2 \text{ m}^2$

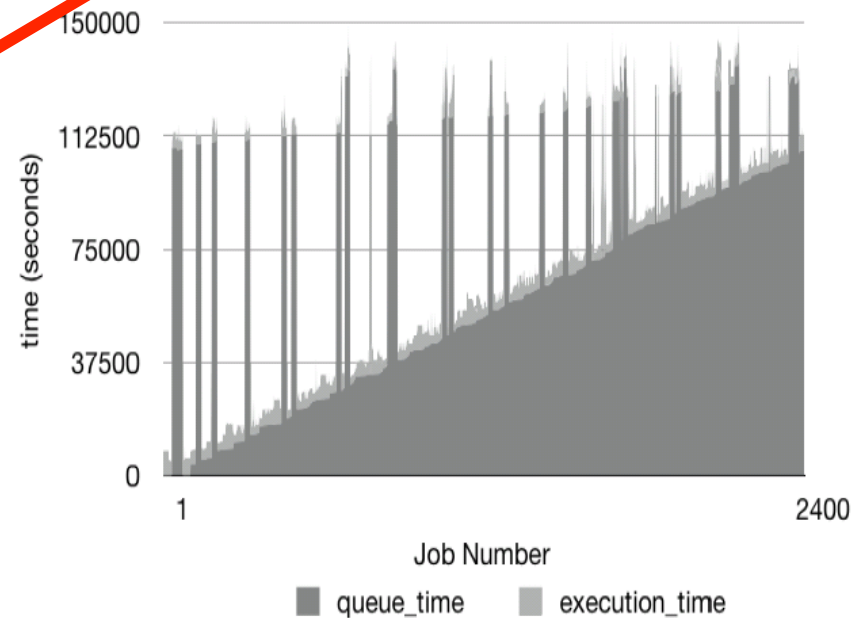


- Comparison

	Version	Slots	Acc. Hours	Speedup
Euler	Optimized	104	1601	86
Grid	Optimized	[90,110]	2998	22

The speedup is calculated from a hypothetical serial version

Ratio of 1.875



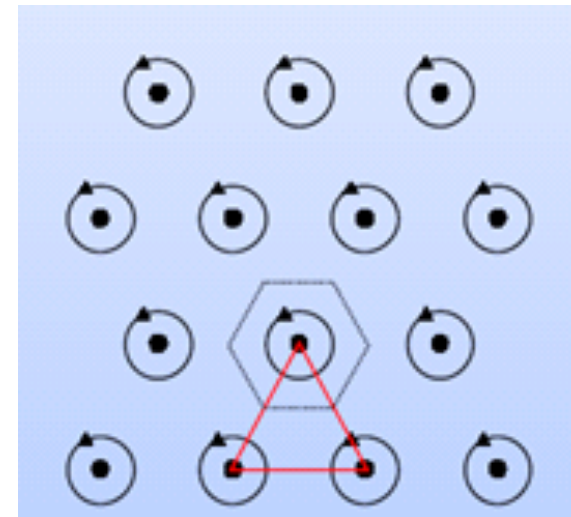
- **Heuristics**

- Not all of them are useful
- “Sum of distances” evaluation on a 60 x 40 lattice and Euler

MF	V_p	S_{Com}/S_{Opt}	Speedup
2	5	1.7	1.0
3	6	13.1	1.3
4	7	25108.2	7.8

- Calculation of U_{ij} from intermediate previous positions
 - Number of candidates is reduced in a 90%...
 - ...but execution time increases in a factor of 4 !!

- **Conclusions**
 - First approach for obtaining vortex lattice dynamics
 - Local clusters and Grid
- **Improvements**
 - Faster migration of Grid jobs (10')
 - New heuristics (SC & Solid State Physics)
 - New lattice geometries
 - Abrikosov
 - Surrounding lattices
 - New interactions
 - Vortex-pinning
 - Temperature



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THANK YOU